# No. UG/108 of 2010

### CIRCULAR: -

A reference is invited to the Ordinances, Regulations and syllabi relating to the Bachelor of Science (B.Sc.) degree course in statistics under the revised pattern vide this Office Circular No. UG/176 of 1999 dated 24th May, 1999 and the Principals of the affiliated colleges in Arts concerned are hereby informed that the recommendation made by the Board of Studies in Statistics at its meeting held on 11th December, 2009 has been accepted by the Academic Council at its meeting held on 3rd March, 2010 vide item No. 4.28 and that in accordance therewith, the syllabus in the subject of Statistics at the T.Y.B.Sc. is revised as per Appendix and that the same has been implemented from the academic year 2010-2011.

MUMBAI-400 032 29<sup>th</sup> May, 2010

(L. R. MANE) offg. REGISTRAR

Го,

The Principals of the affiliated Colleges in Science.

### 1.C/4.28/03.03.2010

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Jo. UG/108-A of 2010

MUMBAI-400 032

28th May, 2010

lopy forwarded with Compliments for information to:-

1. The Dean, Faculty of Science,

- 2. The Chairman, Board of Studies in Statistics.
- 3. The Controller of Examinations,
- 4. The Co-ordinator, University Computerization Centre.

(D. N. JADHAV)

I/c. Deputy Registrar

U.G./P.G.Section.

opy to:-

The Director, Board of College and University Development, the Deputy Registrar (Eligibility and Migration ction), the Director, Board of College and University Development, and Vice-Chancellar, the Pro-Vice-Chancellor, the Eistran and the Director of Students Welfare, the Personal Assistants to the Vice-Chancellar, the Pro-Vice-Chancellor, the gistrar and the Assistant Registrar, Administrative, Ratnagiri for information.

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# UNIVERSITY OF MUMBAI



REVISED SYLLABUS AT T.Y.B.Sc. EXAMINATION IN THE **SUBJECT OF STATISTICS** 

(With effect from the academic year 2010-2011)

# STATISTICS

### PAPER I

# PROBABILITY THEORY AND STOCHASTIC PROCESS

#### PROBABILITY: Unit 1

30L

- i) Theorems on Probability of realization of : a) At least one
- b) Exactly m c) At least m of N events A<sub>1</sub>,A<sub>2</sub>,A<sub>3</sub>,......A<sub>N</sub>. ii) Maxwell Boltzmann, Bose Einstein and Fermi Dirac Statistics.
- iii) Ordered samples and runs.
- iv) Matching and Guessing problems.

Chebychev's theorem, Chebychev's Inequality.

# GENERATING FUNCTIONS:

(Ref. 1,2)

Definitions of generating function and probability generating function. Expression for mean and variance in terms of generating functions. Definition of a convolution of two or more sequences. Generating function of a convolution. Generating functions of the standard discrete distributions. Relation between i) Bernoulli and Binomial distributions ii) Geometric and negative Binomial distributions in terms of convolutions.

#### ORDER STATISTICS: Unit 2

30L

(Ref. 1)

i)Definition of Order Statistics based on a random sample. ii)Derivation of :Cumulative distribution function of the  $\mathbf{r}^{th}$  order statistic. Probability density function of the rth order statistic. Joint Probability density function of the rth and the sth order statistic. Joint Probability density function of all the n ordered statistics. Probability density function of Median (in the case of odd sample sizes) and Range for Uniform and Exponential distributions.

(Ref. 2,3)

#### STOCHASTIC PROCESSES:

Definition of stochastic process. Postulates and difference differential equations for i) Pure birth process ii) Poisson process iii) Yule's process iv)Pure death process v) Death process with  $\mu_n = \mu$  vi) Death process with μ<sub>n</sub>=nμ vii) Birth and death process viii) Linear growth model. Derivation of P<sub>n</sub>(t) for ii), iii), v), vi) Derivation of mean and variance for ii), iii), vi), viii)

(Ref. 1,7)

#### OUEUEING THEORY: Unit 3

30L

Basic elements of the Queueing model. Roles of the Poisson and Exponential distributions. Derivation of Steady state probabilities for the birth and death process. Steady state probabilities and the various average characteristics for the following models

- ii) (M/M/1) : (GD/ N / ∞ ) i) (M/M/1) : (GD/∞/∞)
- iii) (M/M/c) : (GD/ $\infty$  / $\infty$ ) iv) (M/M/c) : (GD/N/ $\infty$ )
- v) (M/M/c) : (GD/ N / N ) c<N vi) (M/M/ $\infty$ ) : (GD/ $\infty$  /  $\infty$ )

Derivation of the waiting time distribution for the (M/M/1):  $(FCFS/\infty/\infty)$ model (Ref. 6)

# Unit 4 BIVARIATE DISTRIBUTIONS

i)Definition and properties of Moment Generating Function of two random variables of continuous and discrete type. Necessary and sufficient condition for independence of two random variables.

### ii) Trinomial distribution;

Definition of joint probability distribution (X,Y). Joint moment generating function, moments  $\mu_{rs}$  where r=0,1,2 and s=0,1,2 Marginal & conditional distributions. Their Means & Variances. Correlation coefficient between the random variables. Distribution of the Sum X+Y.

iii) Extension to Multinomial distribution with parameters  $(n, p_1, p_2, ..., p_{k-1})$  where  $p_1 + p_2, +..., p_{k-1} + p_k = 1$ : Definition of joint probability distribution Concept only.

(iv) Bivariate Normal distribution:

Definition of joint probability distribution (X,Y). Joint moment generating function, moments  $\mu_{rs}$  where r = 0,1,2 and s = 0,1,2 Marginal & conditional distributions. Their Means & Variances. Correlation coefficient between the random variables. Condition for the independence of X and Y. Distribution of aX + bY, where a and b are constants.

Distribution of sample correlation coefficient when  $\rho=0$ . Testing the significance of a correlation coefficient. Fisher's z – transformation. Tests for i)  $H_0: \rho=\rho_0$  and ii)  $H_0: \rho_1=\rho_2$ . Confidence interval for  $\rho$ .

(Ref. 2,3,8)

### TOPICS FOR PRACTICALS:

Ser. No.	Topic
1	Probability
2	Stochastic processes
3	Queueing theory
4	Chebychev's inequality
5	Order statistics
	Generating functions
6	Trinomial & Multinomial distributions
7	
8	Bivariate Normal distribution
9	Significance of correlation coefficient
-	

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- 1. Feller W: An introduction to probability theory and it's applications, Volume:1, Third edition, Wiley Eastern Limited.
- 2. Robert V. Hogg & Allen T. Craig: Introduction to Mathematical Statistics, Fifth edition, Pearson Education (singapore) Pvt Ltd.
- 3. Alexander M Mood, Franklin A Graybill, Duane C. Boes: Introduction to the theory of statistics, Third edition, Mcgraw-Hill Series.
- 4. Hogg R. V. and Tanis E.A.: Probability and Statistical Inference, Fourth edition, McMillan Publishing Company
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- 6. Taha H.A.: Operations Research: An introduction, Eighth edition, Prentice Hall of India Pvt. Ltd.
- 7. J Medhi: Stochastic Processes, Second edition, Wiley Eastern Ltd.
- 8. Biswas S.: Topics in Statistical Methodology (1992), First edition, Wiley Eastern Ltd.
- 9. J. N. Kapur, H. C. Saxena: Mathematical Statistics, Fifteenth edition, S. Chand and Company

## **STATISTICS**

## PAPER- II

### STATISTICAL INFERENCE

	STATISTICAL INFERENCE	
Unit 1	POINT ESTIMATION: Problem of Estimation Definitions of Statistic, Estimator and Estimate	30L
	Properties of a good estimator: Unbiasedness, Consistency.  Efficient estimator, Minimum variance unbiased (MVU) estimator,	
c	Uniqueness property of MVUE. Sufficiency, Neymann Factorization Theorem (without proof) Cramer Rao Inequality, Cramer Rao Lower Bound (CRLB), Definition of	
	Efficient estimator using CRLB (Ref.1)	
Unit 2	METHODS OF ESTIMATION: Method of Maximum Likelihood Estimation (M.L.E.), Properties of M.L.E. Method of Moments	30L
	Method of Minimum Chi-square and Modified Minimum Chi-square (Ref.1)	c
	Prior distribution, Posterior distribution, Loss function, Risk function, Baye's solution under Squared Error Loss Function (SELF) and	
	Absolute Error Loss function. (Ref.1)	
	INTERVAL ESTIMATION: Concept of Confidence Interval and Confidence Limits Definition of pivotal quantity and its use in obtaining confidence limits Derivation of $100(1-\alpha)\%$ equal tailed confidence interval for the parameters $\mu$ , $\mu_1$ - $\mu_2$ (Based on Large and Small samples), $\sigma^2$ , $\sigma_1^2/\sigma_2^2$ of Normal	•
	distribution.  Confidence Intervals based on asymptotic property of m.l.e. for Poisson and Exponential distribution  (Ref. 1)	
Unit 3	TESTING OF HYPOTHESIS: Statistical hypothesis. Problem of testing of hypothesis. Definitions and	301
	Hypothesis iv) Alternative Hypothesis vyrest of significance ix) p-value region vii) Type I and Type II errors viii) Level of significance ix) p-value x) size of the test xi) Power of the test xii) Power function of a test	•
	xiii) Power curve.  Definition of most powerful test of size α for a simple hypothesis against a simple alternative hypothesis. Neyman –Pearson fundamental lemma.	

Definition of uniformly most powerful (UMP) test. Construction of UMP

test for one tailed alternative hypothesis.

(Ref. 1,2,6)

# LIKELIHOOD RATIO TEST:

Likelihood ratio principle. Definition of the test statistic and its asymptotic distribution (statement only) Derivation of the test procedure for testing a composite hypothesis against a composite alternative hypothesis for the parameters  $\mu$  and  $\sigma^2$  of Normal distribution.

(Ref. 1)

Unit 4 NON PARAMETRIC TESTS:

30 L

Need for non parametric tests. Distinction between a parametric and a non parametric test. Advantages and Disadvantages of Non-Parametric Tests. Single sample and double sample nonparametric tests. i) Sign test ii) Wilcoxon's signed rank test.iii) Median test iv) Mann – Whitney –Wilcoxon test.v) Run test. Assumptions, justification of the test procedure, critical regions for one tailed and two tailed test procedures. Problems with no ties.

(Ref. 3)

# SEQUENTIAL PROBABILITY RATIO TEST:

Sequential probability ratio test procedures for testing a simple null hypothesis against a simple alternative hypothesis. Its comparison with fixed sample size. Neyman- Pearson test procedure. Definition of Wald's SPRT of strength  $(\alpha, \beta)$ . Problems based on standard distributions: Bernoulli, Poisson, Normal, Exponential. Graphical and tabular procedures for carrying out the tests.

(Ref. 1, 4)

# TOPICS FOR PRACTICALS:

Ser. No.	Topic
1	Method of Moments
2	Method of Maximum Likelihood
3	Method of Modified Minimum Chi-square
4	Bayesian Estimation
5	Interval Estimation
6	Testing of Hypotheses
7	Likelihood Ratio Tests
8	Non Parametric Tests
9	Sequential Probability Ratio Test

#### REFERENCES:

- 1. Hogg R.V. and Craig A.T: Introduction to Mathematical Statistics, Fourth edition, London Macmillan Co. Ltd.
- 2. Hogg R.V. and Tanis E.A.: Probability and Statistical Inference, Third edition, Delhi Pearson Education.
- 3. Daniel W.W.: Applied Non Parametric Statistics, First edition, Boston-Houghton Mifflin Company
- 4. Wald A.: Sequential Analysis, First edition, New York John Wiley & Sons
- 5. Biswas S.: Topics in Statistical Methodology, First edition, New Delhi Wiley eastern
- 6. Gupta S.C. and Kapoor V.K.: Fundamentals of Mathematical Statistics, Tenth edition,
  New Delhi S. Chand & Company Ltd.

# STATISTICS

# PAPER III

# <u>APPLIED STATISTICS - I</u>

#### EPIDEMIC MODELS: Unit 1

30L

The features of Epidemic spread. Definitions of various terms involved. Simple mathematical models for epidemics: Deterministic model without removals. Deterministic model with removals. Threshold theorem. Host - vector model. Modified Threshold theorem. Carrier model. Chain binomial models. Reed – frost and Greenwood models. Distribution of individual chains and total number of cases. Maximum likelihood estimator of p and its asymptotic variance for the households of sizes up to 4. (Ref.1)

#### BIOASSAYS: Unit 2

30L

Meaning and scope of bioassays. Relative potency. Direct assays. Fieller's theorem .Indirect assays. Dose-response relationship .Condition of similarity and Monotony. Linearizing transformations. Parallel line assays. Symmetrical 2K-point parallel line assays (K=2,3). Validity tests using orthogonal contrasts .Quantal assays. Tolerance distribution. Median effective dose ED50 and LD50. Probit analysis.

### CLINICAL TRIALS:

(Ref.2,3)

Introduction to clinical trials: The need and ethics of clinical trials. Over view of phases (I-IV)

Common terminology used in clinical trials

Study Protocol, Case record/Report form, Blinding (Single/double)

Randomised controlled (Placebo/active controlled)

Study Designs (Parallel, Cross Over)

Types of Trials: Inferiority, Superiority and Equivalence, Multicentric

Trial. Inclusion/Exclusion Criteria

Statistical tools: Analysis of parallel Design using Analysis of Variance.

Concept of odds ratio. Sample size estimation.

(Ref.4,5,6,7)

## Unit 3

30L

Deterministic Models: Single item static EOQ models for i) Constant raic of demand with instantaneous replenishment, with and without shortages. ii) Constant rate of demand with uniform rate of replenishment, with and without shortages. iii) Constant rate of demand with instantaneous replenishment without shortages, with at most two price breaks. Probabilistic models. - Single period with i) Instantaneous demand (discrete and continuous) without setup cost. ii) Uniform demand (discrete and continuous) without set up cost. (Ref 9, 12, 13)

### GAME THEORY:

Definitions of Two person Zero Sum Game, Saddle Point, Value of the Game, Pure and Mixed strategy.

Optimal solution of two person zero sum games: Dominance property, Derivation of formulae for (2 x 2) game. Graphical solution of (2 x n) and (m x 2) games.

(Ref. 9)

#### Unit 4 REPLACEMENT:

30L

Replacement of items that deteriorate with time and the value of money i) remains constant ii) changes with time using weighted average of costs. Replacement of items that fail completely. Individual replacement and Group replacement policies.

(Ref.13)

#### **DECISION THEORY:**

Decision making under uncertainty Laplace criterion, Maximax (Minimin) criterion, Maximin (Minimax) criterion, Hurwicz α criterion, Minimax Regret criterion.

Decision making under risk: Expected Monetary value criterion, Expected Opportunity Loss Criterion, EPPI, EVPI. Bayesian Decision rule for Posterior analysis. Decision tree analysis along with Posterior probabilities.

(Ref.9)

### TOPICS FOR PRACTICALS:

Ser. No.	Topic
1	Deterministic epidemic models
2	Chain Binomial models
3	Direct Assays
1	Parallel line Assay .
5	Quantal Assays
5	Clinical Trials
1	Deterministic inventory models
3	Probabilistic inventory models
)	Game Theory
0	Replacement
11	Decision Theory

#### REFERENCES:

- Bailey N.T.J.: The Mathematical theory of infectious diseases, Second edition, Chrles Griffin and Co. London
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- 5. Zar Jerrold H.: Biostatistical Analysis, Fourth edition, Pearson's education
- Friedman L. M., Furburg C., Demets D. L. (1998): Fundamentals of Clinical Trials, First edition, Springer Verlag.
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- S. D. Sharma: Operations Research, Eighth edition, Kedarnath Ramnath & Co.

# **STATISTICS**

# PAPER IV

# <u>APPLIED STATISTICS - II</u>

#### MORTALITY TABLES: Unit 1

30L

Various mortality functions. Probabilities of living and dying. The force of mortality. Estimation of  $\mu_x$  from the mortality table. Laws of mortality: Gompertz's and Makeham's first law. Select and Ultimate mortality tables. Mortality table as a population model. Stationary population. Expectation of life and Average life at death. Central death rate.

(Ref.1,2)

# COMPOUND INTEREST AND ANNUITIES CERTAIN:

Accumulated value and present value, nominal and effective rates of interest. Discount and discounted value, Varying rates of interest. Equation of value. Equated time of payment.

Present and accumulated values of annuity certain (immediate and due) with and without deferment period.

Present value for perpetuity (immediate and due) with and without deferment period

Present and accumulated values of i) increasing annuity iii)increasing annuity when successive installments form a) arithmetic progression b) geometric progression. iv) annuity with frequency different from that with which interest is convertible.

Present value for increasing perpetuity (immediate and due). Redemption of loan.

(Ref.2)

#### Unit 2 **ASSURANCE BENEFITS:**

30L

Present value of Assurance benefits in terms of commutation functions of i) pure endowment assurance ii) temporary assurance iii) endowment assurance iv) whole life assurance v) double endowment assurance vi) increasing temporary assurance viii) increasing whole life assurance viii) special endowment assurance ix) deferred temporary assurance x) deferred whole life assurance.

Present value in terms of commutation functions of Life annuities and Temporary life annuities (immediate and due) with and without deferment period. Present values of Variable and increasing life annuities(immediate and due)

Net premiums and Level annual premiums for the various assurance plans. Natural premiums. Office premiums.

(Ref1,2)

#### Unit 3 TIME SERIES:

30L

Definition of Time series. Its components. Models of Time Series. Estimation of trend by i) Freehand curve method ii) Method of semi averages iii) Method of moving averages iv) Method of least squares.

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v) Exponential smoothing method

Estimation of seasonal component by i) Method of simple averages

ii) Ratio to moving average method iii) Ratio to trend method

(Ref.3,4)

#### SIMULATION:

Scope of simulation applications. Types of simulation. Monte Carlo Technique of Simulation. Elements of discrete event simulation. Generation of random numbers. Sampling from probability distribution. Inverse method. Generation of random observations from i) Uniform distribution ii) Exponential distribution iii) Gamma distribution iv) Normal distribution. Simulation techniques applied to inventory and Oucueing models.

(Ref.6)

#### RELIABILITY: Unit 4

30L

Concept of reliability, Hazard-rate. Bath tub curve. Failure time distributions :i) Exponential ii) Gamma iii) Weibull iv) Gumbel. Definitions of increasing (decreasing) failure rate. System Reliability Reliability of i)series ii) parallel system of independent components having exponential life distributions. Mean Time to Failure of a system (MTTF).

(Ref 8,9)

## LINEAR REGRESSION:

Linear regression model with one or more explanatory variables. Assumptions of the model, Derivation of ordinary least square (OLS) estimators of regression coefficients, (for one and two explanatory variables models) Properties of least square estimators (without proof) Coefficient of determination R<sup>2</sup> and adjusted R<sup>2</sup>. Procedure of testing i) overall significance of the model ii) significance of individual coefficients iii) significance of incremental contribution of explanatory variable for two explanatory variables model. Confidence intervals for the regression coefficients.

Autocorrelation: Concept, Detection using i) Run Test ii) Durbin Watson

Test, Generalized least square (GLS) method.

Heteroscedasticity: Concept, Detection using i) Spearman's rank correlation test. ii) Breusch-Pagan-Godfrey test. Weighted least square

Multicollinearity: Concept, Detection using i) R square & t ratios ii) pair wise correlation between regressors iii) Variance Inflation Factor

Consequences of using OLS estimators in presence of autocorrelation,

heteroscedasticity and multicollinearity. (Ref.10,11)

### TOPICS FOR PRACTICALS:

Ser. No.	Topic
1	Mortality tables .
2	Annuities
3	Life annuities
4	Assurance benefits
5	Time series
6	Simulation
7	Reliability
8	Multiple regression model
9	Autocorrelation, Heteroscedasticity, Multicollinearity

#### REFERENCES:

- Neill A.: Life Contingencies, First edition, Heineman educational books London
- 2. Dixit S.P., Modi C.S., Joshi R.V.: Mathematical Basis of Life Assurance, First edition Insurance Institute of India
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  Analysis of Reliability and Life Data, First edition, John Wiley & Sons
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